

# Tributes

Volume 23

## Infinity, Computability, and Metamathematics

Festschrift celebrating the 60<sup>th</sup> birthdays of  
Peter Koepke and Philip Welch

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Proofs, Categories and Computations. Essays in Honour of Grigori Mints  
Solomon Feferman and Wilfried Sieg, eds.

Volume 14

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60<sup>th</sup> Birthday  
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Volume 22

Foundational Adventures. Essays in Honour of Harvey M. Friedman  
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Stefan Geschke, Benedikt Löwe and Philipp Schlicht, eds.

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# Infinity, Computability, and Metamathematics

Festschrift celebrating the 60<sup>th</sup> birthdays of  
Peter Koepke and Philip Welch

edited by

Stefan Geschke

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Philipp Schlicht

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# Table of Contents

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Table of Contents .....	v–vi
Preface .....	vii–viii
Publications by Peter Koepke .....	ix–xiv
Publications by Philip Welch .....	xv–xx
Doctoral students .....	xxi
A note on powers of singular strong limit cardinals	
<i>A. Apter</i> .....	1–3
The consistency of a club-guessing failure at the successor of a regular cardinal	
<i>D. Asperó</i> .....	5–27
A survey of axiom selection as a machine learning problem	
<i>J. C. Blanchette, D. Kühnwein</i> .....	29–48
The lost melody phenomenon	
<i>M. Carl</i> .....	49–70
Modelling the usage of partial functions and undefined terms using pre-supposition theory	
<i>M. Cramer</i> .....	71–88
The foundation axiom and elementary self-embeddings of the universe	
<i>A. S. Daghighi, M. Golshani, J. D. Hamkins, E. Jeřábek</i> .....	89–112
Sets of good indiscernibles and Chang conjectures without choice	
<i>I. Dimitriou</i> .....	113–137

An ordinal $\lambda$ -calculus	
<i>T. Fischbach, B. Seyffferth</i> .....	139–166
Coding over core models	
<i>S.-D. Friedman, R. Schindler, D. Schrittesser</i> .....	167–182
Extender based forcings, fresh sets and Aronszajn trees	
<i>M. Gitik</i> .....	183–203
On ground model definability	
<i>V. Gitman, T. A. Johnstone</i> .....	205–227
On the automorphisms in the Gitik-Koepke construction	
<i>V. Kanovei</i> .....	229–253
On compactness for being $\lambda$ -collectionwise Hausdorff	
<i>M. Magidor</i> .....	255–272
Cardinal sequences for superatomic Boolean algebras	
<i>J. C. Martínez</i> .....	273–284
One-dimensional $\Sigma$ -presentations of structures over $\mathbf{HF}(\mathbb{R})$	
<i>A. Morozov</i> .....	285–298
Remarkable cardinals	
<i>R. Schindler</i> .....	299–308
The weak ultimate $\mathbf{L}$ conjecture	
<i>W. H. Woodin</i> .....	309–329

## Preface

In the year 2014, Peter Koepke and Philip Welch turned sixty and we celebrated this festive occasion with a scientific workshop in their honour. The workshop speakers included students, collaborators, colleagues, and friends of Peter and Philip whose research was influenced by them.



Peter and Philip have more in common than their age. Both were professors at the University of Bonn; Peter for many years and Philip as a Mercator Professor during the academic year 2002/3. Both were strongly influenced by Ronald Jensen early in their scientific careers. Philip got his D.Phil. in 1979 from the University of Oxford under the supervision of Robin Gandy with a thesis on combinatorial principles in Jensen's core model, with Jensen being in Oxford from 1978 to 1979. Peter received his doctoral degree from the University of Freiburg under Jensen's supervision with a dissertation titled "A Theory of Short Core Models and Some Applications". Peter and Philip continued working in set theory, but they also got interested in other subjects in logic: infinite time computation is another of these interests that they shared. In the last two decades, their interests became increasingly interdisciplinary: Philip started working with philosophers on theories of truth and Peter collaborated with linguists on natural language proofs. Three joint publications witness their common interests.

This Festschrift was handed over to Peter and Philip on 23 May 2014 during the Colloquium and Workshop "Infinity, computability, and metamathematics: Celebrating the 60th birthdays of Peter Koepke and Philip Welch", which took place from 23 May to 25 May 2014 at the Hausdorff Center for Mathematics (HCM) at the *Rheinische Friedrich-Wilhelms-Universität*

*Bonn.* The workshop and the production of the book were funded by the HCM. We received nineteen submissions for this Festschrift which were thoroughly refereed according to the standards of our field; nineteen referees helped us with this in very short time (we received the first submissions in late September 2013 and needed to submit the volume for production in April 2014; readers who know the usual glacial pace of mathematical publishing can appreciate how fast this is) and in the end, seventeen papers were accepted for publication in the Festschrift. As is traditional, we included lists of the publications and doctoral students of Peter and Philip in this preface to document their important role in our community. We are very happy to see five of the doctoral students among the authors of papers in this Festschrift. We should like to thank all authors and referees for their collaboration in producing this interesting book and hope that Peter and Philip will enjoy it.

April 2014, Hamburg, Amsterdam, and Bonn

S. G. B. L. P. S.



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